

## Round Table Activity

Simplify:

1. $\sqrt{-60}$ $= \sqrt{-1} \cdot \sqrt{4} \cdot \sqrt{15}$ $= 2i\sqrt{15}$	2. $\sqrt{128}$ $\sqrt{2} \cdot \sqrt{64}$ $8\sqrt{2}$
3. $\sqrt{-81}$ $= \sqrt{81} \cdot \sqrt{-1}$ $= 9i$	4. $\sqrt{32}$ $= \sqrt{16} \cdot \sqrt{2}$ $= 4\sqrt{2}$

### 5.2L Solving Quadratic Equations Using the Quadratic Formula to Find Real Solutions

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Section  
5.2L

#### Is it factorable?

To determine if a quadratic equation is factorable, find the value of the discriminant.

- If the **discriminant** is a **perfect square number OR zero**, then the quadratic equation **is factorable**
- If the **discriminant** is **not a perfect square number OR negative**, then the quadratic equation **is not factorable**.

#### The Quadratic Formula

Let  $a$ ,  $b$ , and  $c$  be real numbers such that  $a \neq 0$ . The solutions of the quadratic equation  $ax^2 + bx + c = 0$  are:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \rightarrow \text{disc}$$

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DISCRIMINANT:

$$b^2 - 4ac$$

The discriminant determines the number and type of solutions of any quadratic (remember to set the equation = 0 first).

What is a solution/root/zero? \_\_\_\_\_

Discriminant    # of roots    types of roots

**-Positive**                      **2**                      **real**

(if the discriminant is a perfect square the roots are rational and the equation can be factored...and if not a perfect square the roots are irrational)

**-Zero**                              **1**                      **real**

(this is called a double root...where the graph "bounces" off of the x-axis)

**-Negative**                      **0**                      **real**

(no real roots means there must be 2 complex or imaginary)

Simplify: **RPEMDAS**

$x = \frac{6 \pm \sqrt{16}}{2}$ <p>Disc = <b>16</b> #Type of solutions = <b>2 real rational</b></p> $x = \frac{6 \pm 4}{2}$ $x = \frac{3 \pm 2}{1} = 3 \pm 2$ $x = 3+2 = 5$ $x = 3-2 = 1$	$x = \frac{-5 \pm \sqrt{-8}}{4}$ <p>Disc = <b>-8</b> #Type of solutions = <b>2 complex</b></p> <p>Note: <math>\sqrt{-8} = \sqrt{1 \cdot 8} = \sqrt{1} \cdot \sqrt{8} = 1 \cdot 2\sqrt{2} = 2i\sqrt{2}</math></p> $x = \frac{-5 \pm 2i\sqrt{2}}{4}$ $x = \frac{-5 + 2i\sqrt{2}}{4}$ $x = \frac{-5 - 2i\sqrt{2}}{4}$
$x = \frac{-9 \pm \sqrt{32}}{6}$ <p>Disc = <b>32</b> #Type of solutions = <b>2 real irrational</b></p> $x = \frac{-9 \pm 4\sqrt{2}}{6}$ $x = -\frac{9}{6} \pm \frac{4\sqrt{2}}{6}$ $x = -\frac{3}{2} \pm \frac{2\sqrt{2}}{3}$ $x = -\frac{3}{2} + \frac{2\sqrt{2}}{3}$ $x = -\frac{3}{2} - \frac{2\sqrt{2}}{3}$	$x = \frac{-28 \pm \sqrt{0}}{14}$ <p>Disc = <b>0</b> #Type of solutions = <b>1 real rational</b></p> $x = \frac{-28 \pm 0}{14}$ $x = -\frac{28}{14} = -2$ $x = -2$

Use the quadratic formula to solve the following equation.

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1) Solve  $9x^2 + 6x = 1$

Step 1: Write the equation in standard form.

Step 2: Identify the values of  $a$ ,  $b$  and  $c$ .

$a = 9$   $b = 6$   $c = -1$

Step 3: Substitute the values from Step 2 into the quadratic formula and simplify.

$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$x = \frac{-6 \pm \sqrt{72}}{18}$

$x = \frac{-6 \pm 6\sqrt{2}}{18 \div 6}$

$x = \frac{-1 \pm 1\sqrt{2}}{3}$

$x = \frac{-1 + \sqrt{2}}{3}$        $x = \frac{-1 - \sqrt{2}}{3}$

$b^2 - 4ac$   
 $(6)^2 - 4(9)(-1) = 36 - (-36)$   
 $= 36 + 36$   
 $= 72$   
 ↓  
 2 Real + Irrational

#2 - 5: Use the quadratic formula to find the solutions to the following equations.

4)  $x^2 + 10x = -22$

Disc: 12  
 $x = -5 + \sqrt{3}$   
 $x = -5 - \sqrt{3}$

5)  $2x + 9 = 7x^2$

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Disc: 256  
 $x = -1$   
 $x = 9$